

# Application of Attribute Graph Grammars to Syntactic Editing of Tabular Forms

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# Terms

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- **Tabular forms with syntax**
- **Graph grammars** for tabular form syntax
- **Attribute** : used for drawing
- **edNCE** : edge-direct Neighbourhood Controlled Embedding  
(cf. NLC : Node Labeled Controlled) :  
A type of embedding mechanisms of right hand side graph into host graph for **graph rewriting**
- **Syntactic editing** : editing defined by sequence of rewriting rules



# Types of Visual Data (ex. Power Point)

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- Character String
- Tree Diagrams
- **Tabular Forms (Our Target)**
  - **Modular Tabular Form**
  - **Tessellation Tabular Form**
- Graphs
- Images

## ■ Target

Project Code:	
Program Name:	
Library Code:	Version:
Author:	Original Release:
Approver:	Current Release:
Problem Description:	
Problem Supplementary Information (Theoretical Principles, Methods and References):	
Problem Solution: 1.Conventions and Terminology 2.Principles and Algorithms	

Modular Tabular Form

Name	Type	Size	G/L
x	int	2	G
y	float	4	L

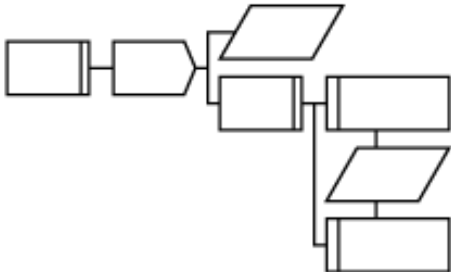
Tessellation Tabular Form

## ■ Goals

Constructing the **syntactic editing mechanisms** of tabular forms based on attribute graph grammar.

# 1. Introduction

## Positions of this Paper

	CPS	Flowcharts	Program Specification						
<b>Diagrams</b>	string	Hierarchical Diagram 	Modular Diagram <table border="1" data-bbox="1214 622 1877 873"> <tr> <td colspan="2">Program Code:</td> </tr> <tr> <td colspan="2">Program Name:</td> </tr> <tr> <td>Library Code:</td> <td>Version:</td> </tr> </table>	Program Code:		Program Name:		Library Code:	Version:
Program Code:									
Program Name:									
Library Code:	Version:								
<b>Representation</b>	string	Attribute Tree	Attribute Marked Tree						
<b>Syntax</b>	CFG	Attribute CFGG (Yaku, Tsuchida et al)	Attribute NCE CFGG (Arita et al)						
<b>Editor Command</b>	○	○ (Yaku, Tsuchida, et al)	<b>This Paper</b>						

# Background

## Models

### Graph Grammars

Precedence Graph Grammars  
(Franck 1978)

Attribute Graph Grammars  
(Nishino 1989)

Precedence Attribute Graph Grammars  
(Arita et al,  
IASTED AI2001)

### Syntax-Direct Editors

CPS  
(Teitelbaum et al 1981)

Syntactic Diagram Editing  
(Yaku, et al 1993)

## Application

### Tables

Table in WORD  
Table in HTML

Marked Graph  
for Modular Tables  
(Tomiyaama, Arita, et al  
IFIP WCC2000)



# Why Graph Grammars

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- Tabular Forms have syntax
- To determine the scope of rewriting by cell deletion or insertion
- Without graph grammars, often to collapse whole structure of tables



# Why Attribute Graph Grammars

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- Rewriting scope determined by graph grammars.
- Attribute rules concerned to graph grammars
- Incremental drawing





# Motivation

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- To investigate whether graph grammars can effectively formalize table processing.



# Purpose

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- Formalization of editing by graph grammars
- Properties of editing model
- Algorithms of editing by graph grammars
- Attribute evaluation for drawing



# Results

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- Definitions of deletion, insertion by rewriting rules of edNCE graph grammars
- Confluence of editing
- Linear time algorithm with attribute evaluation for primitive drawing conditions



# Related Works

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- Related works for **syntactic editing methods** are **CPS**, **DIAGEN**(Minas et al.) and so on.

# 2 . Preliminaries

# 2. Preliminaries

program specification  
language

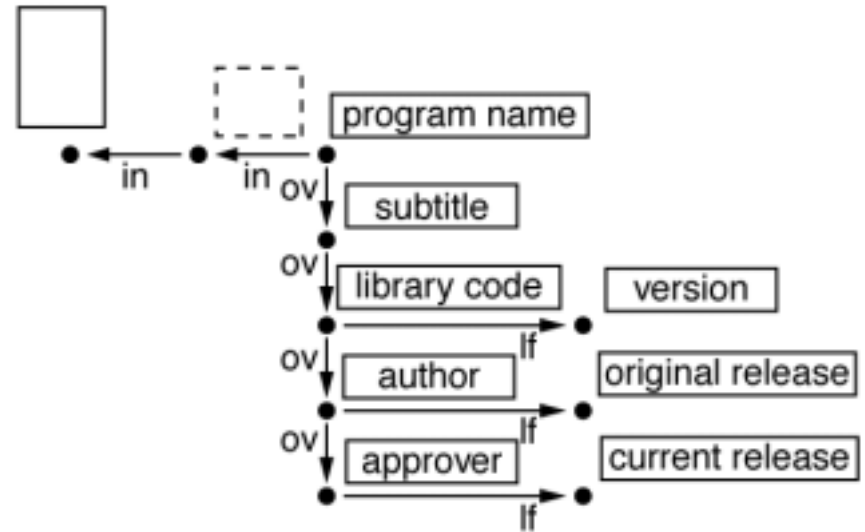
- 17 types of Forms based on ISO6592
- A collection of tabular forms

<b>program name</b> : Hanoi_main	<b>A</b> <b>General document</b>
<b>subtitle</b> : hanoi	
<b>library code</b> : cs - 2000 - 01	<b>version</b> : 1.0
<b>author</b> : Kiyonobu Tomiyama	<b>original release</b> : 1999/12/22
<b>approve</b> :	<b>current release</b> : 2000/01/28
<b>key words</b> : Hanoi Tower	<b>CR-code</b> :
<b>scope</b> : Fundamental	
<b>varlant</b> :	
<b>language</b> : Java	<b>software req.</b> : JDK 1.2
<b>operation</b> : Interactive batch realtime	<b>hardware req.</b> :
<b>references</b> :	
<b>function</b> : 1. list and explanation of input data or parameter, 2. list and explanation of output data or return value.	
1. list and explanation of input data.	
int n; [ Number of Plates ] String target; [ Target Symbol ] String work; [ Working Symbol ] String destination; [ Destination Symbol ]	
2. list and explanation of output data and return value.	
output data : No. to be moved: Source Symbol -> Destination Symbol return value : void	
<b>example</b> :	
1. Example of Operation	
hanoi(5, A, B, C)	
2. Example of Output	
1: A -> C 2: A -> B 1: C -> B 3: A -> C 1: B -> A .....	

# Modular Tabular Form and Its Corresponding Marked Graph

program name :	
subtitle :	
library code :	version :
author :	original release :
approver :	current release :

program name :	
subtitle :	
library code :	version :
author :	original release :
approver :	current release :



# 2.1 An Attribute edNCE Graph Grammar

## 2.1.1 Definition

An attribute NCE graph grammar is a 3-tuple  $AGG = \langle G, Att, F \rangle$

1.  $G = (\Sigma, \Delta, \Gamma, \Omega, P, S)$  is an underlying graph grammar of  $AGG$ .
2.  $Att = \bigcup_{Y \in V} Att(Y)$ ,  
( $Att(Y) = Inh(Y) \cup Syn(Y)$ .)
3.  $F = \bigcup_{p \in P} F_p$  is the set of semantic rules of  $AGG$ .





## 2.1 edNCE Graph Grammar[6]

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### Definition 2.1.1

edNCE graph grammar:  $G = (N, T, E, F, P, S)$  where

$N$ : The alphabet of node labels

$T$ : The alphabet of terminal node labels

$E$ : The alphabet of edge labels

$F$ : The alphabet of final edge labels

$P$ : The finite set of productions

$S$  -  $s \in N$ : The initial nonterminal



# edNCE Graph Grammar (continued)

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production  $p : X \quad (D,C)$

$X$  -

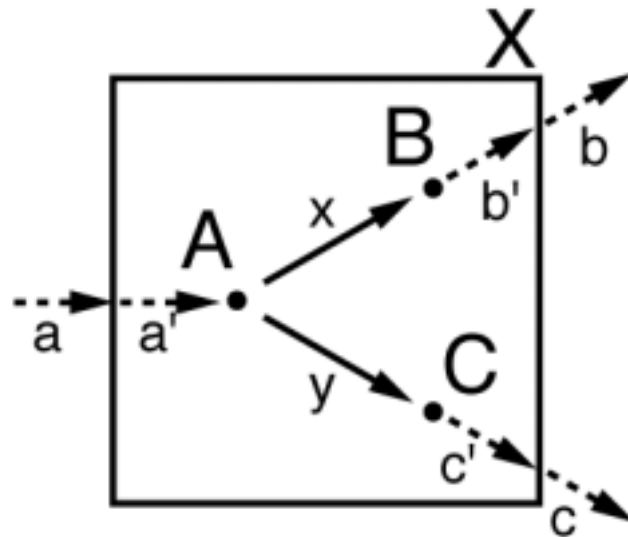
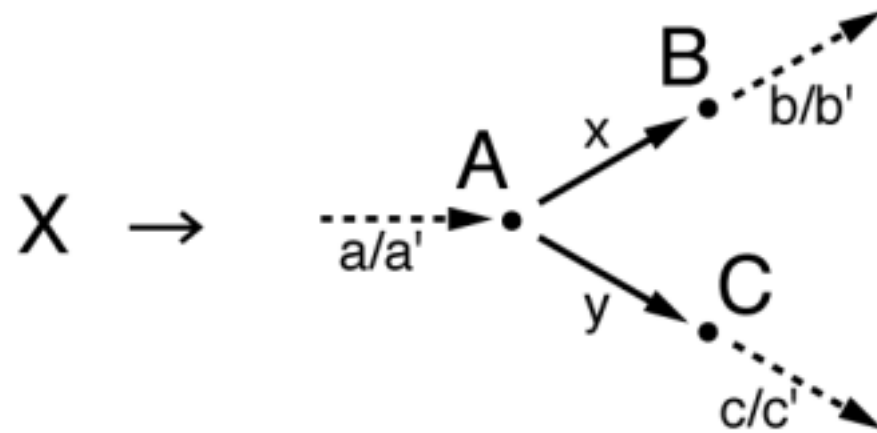
$(D,C)$  GRE ,

$D$  GR ,

$C$   $\times \times \times V_D \times \{in,out\}$

: connection relation

# Production



# 2.2 COMPOSITION OF PRODUCTION COPIES [4]

## 2.2.1 Definition

Let  $G = (V, \Sigma, P, S) : \text{edNCE-CFG}$

$p_1 : X_1 (D_1, C_1), p_2 : X_2 (D_2, C_2) : \text{production copy of } G,$

for  $X_2$  exists in node labels of  $D_1$

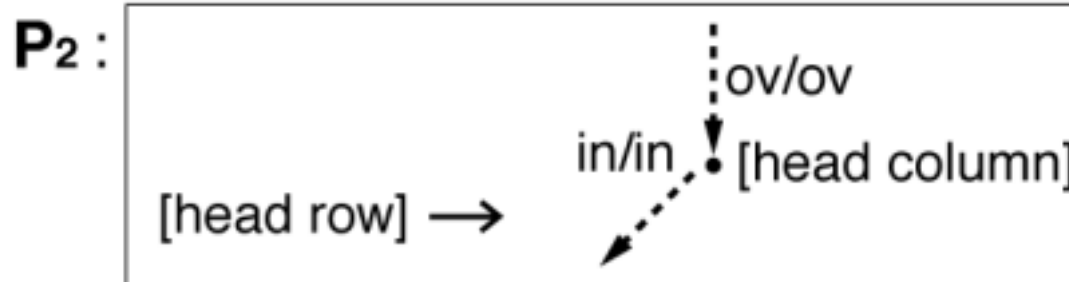
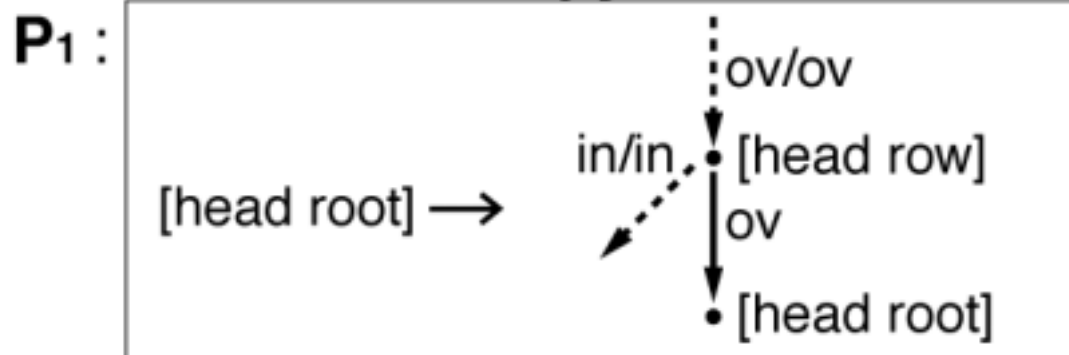
The composite production copy  $p : X_1 (D, C),$   
where

$$D = D_1 - \{X_2\} \cup D_2$$

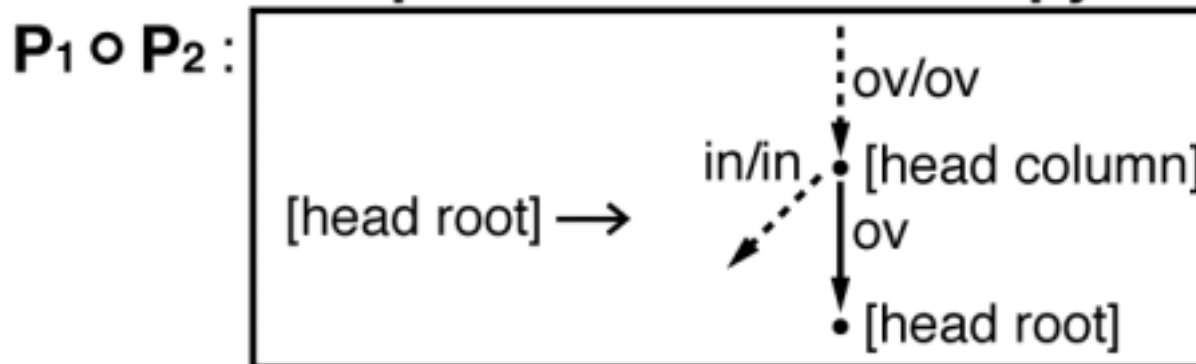
$$C = \{ (x, y, d) \in C_1 \mid x \in V_{D_1} - V_{X_2} \} \cup \{ (x, y, d) \in C_2 \mid x \in V_{X_2} \}$$

## ■ Example (Composite Production copy)

### Production Copy



### Composite Production Copy





## 2.3 Confluence Property [6]

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### Definition 2.3.1

An edNCE graph grammar  $G=(\quad, \quad, \quad, \quad, P, S)$  is confluent if the following holds for every sentential form  $H$  of  $G$ :

If  $H \Rightarrow_{u_1, p_1} H_1 \Rightarrow_{u_2, p_2} H_{12}$  and  $H \Rightarrow_{u_2, p_2} H_1 \Rightarrow_{u_1, p_1} H_{21}$  ( $p_1, p_2$

$P$ )

are derivation of  $G$  with

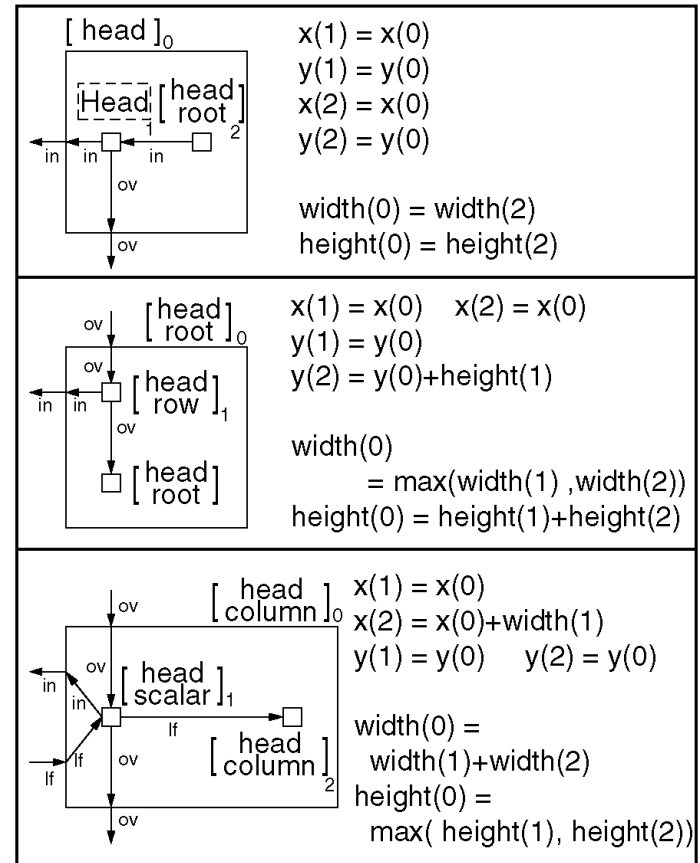
$u_1, u_2 \quad \forall H$  and  $u_1 \quad u_2$ ,

then  $H_{12}=H_{21}$

# HNGG (Hiform Nested Form Graph Grammar)

<b>Graph grammar</b>	<b>HNGG</b>
<b>productions</b>	<b>280</b>
<b>attribute rules</b>	<b>1248</b>
<b>precedence relations</b>	<b>5376</b>

## Production Examples of HNGG



# 3 Editing of Modular Tabular Form





# 3.1 Production Instance

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## 3.1.1 Definition

A production instance is a 3-tuple  $(\omega, p_i, H'_{p_i})$ ,  $\stackrel{\text{def}}{\iff}$

1.  $\omega \in V_{D_{i-1}}$  is a node removed during the derivation  $D_{i-1} \Rightarrow_{p_i} D_i$ .
2.  $p_i : X_{p_i} \rightarrow (H_{p_i}, C_{p_i}) \in P$  is a production.
3.  $H'_{p_i}$  is an embedded graph isomorphic to  $H_{p_i}$  during  $D_{i-1} \Rightarrow_{p_i} D_i$ .

We denote  $D_{i-1} \xrightarrow[p_i]{\omega H'_{p_i}} D_i$

if  $D_{i-1}$  is directly derived  $D_i$  by applying the instance  $(\omega, p_i, H'_{p_i})$ .

## 3.2 Syntactic Insertion

# 3.2 Syntactic Insertion

## 3.2.1 Definition

For an derivation sequence

$$D_0 \xRightarrow{\omega_1 H'_{p_1}} \cdots \xRightarrow{\omega_{i-1} H'_{p_{i-1}}} D_{i-1} \xRightarrow{\omega H'_{p_i}} D_i \xRightarrow{\omega_{i+1} H'_{p_{i+1}}} \cdots \xRightarrow{\omega_n H'_{p_n}} D_n$$

$(p_j : X_{p_j} \rightarrow (H_{p_j}, C_{p_j}), 1 \leq j \leq n)$ ,  $q$  is insertable (for  $p_i$ )

$\Leftrightarrow$   
*def*

there is an instance  $(\omega, q, H'_q)$  ( $q : X_q \rightarrow (H_q, C_q) \in P_N$ )

s.t.  $D_{i-1} \xRightarrow{\omega H'_q} Q$ ,

there is a derivation sequence

s.t.  $D_{i-1} \xRightarrow{\omega H'_q} Q \xRightarrow{\omega' H'_{p_i}} D'_i \xRightarrow{\omega_{i+1} H'_{p_{i+1}}} \cdots \xRightarrow{\omega_n H'_{p_n}} D'_n$ .



1. Trace the derivation sequence  $D_n$  back to  $D_{i-1}$ .
2. Apply the instance  $(\omega, q, H'_q)$  to  $D_{i-1}$ , and obtain the resultant graph  $Q$ .
3. Apply the instance sequence  $((\omega'_i, p_i, H'_{p_i}), (\omega'_{i+1}, p_{i+1}, H'_{p_{i+1}}), \dots, (\omega'_n, p_n, H'_{p_n}))$  to  $Q$ , and get the resultant graph  $D'_n$ .

□

insertable by composite production copy is similarly defined.

### 3.2.3 Definition

A graph  $H'$  is obtained by syntactic insertion of a graph  $A$  at an edge  $x$  in a graph  $H$ .

$\iff$   
*def*

1. A composite production copy  $q$  for the graph  $A$  and an edge  $x$  exists.
2. There exists an instance sequence  $i_q$  for  $q$  and an instance sequence  $i_H$  for  $H$ .  
An instance sequence  $S$  is obtained by insertion of  $i_q$  into  $i_H$ .
3.  $H'$  is derived by  $S$ .

□

### 3.2.4 Proposition

Let  $H$  be the graph obtained from  $G$  by the insertion of nodes  $a$  and  $b$  at edge  $x$  and edge  $y$  respectively in this order, in HNGG. Let  $H'$  be the graph obtained from  $G$  by the insertion of nodes  $b$  and  $a$  at edge  $y$  and edge  $x$  respectively in this order, in HNGG.

$\iff$

$$H = H'.$$

**Proof** HNGG has confluence property. Thus, the theorem is verified.

□

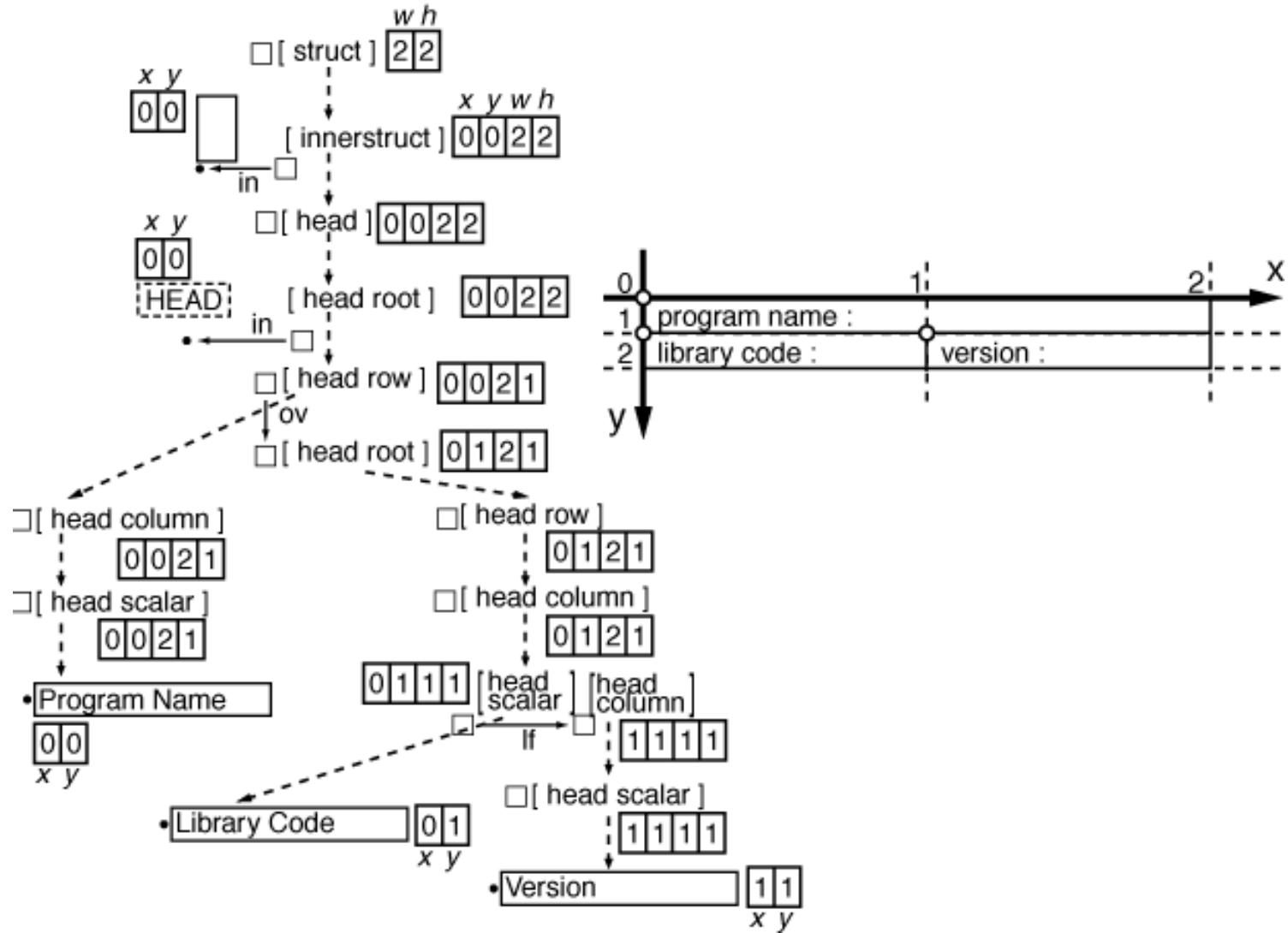
### **3.2.5 Proposition**

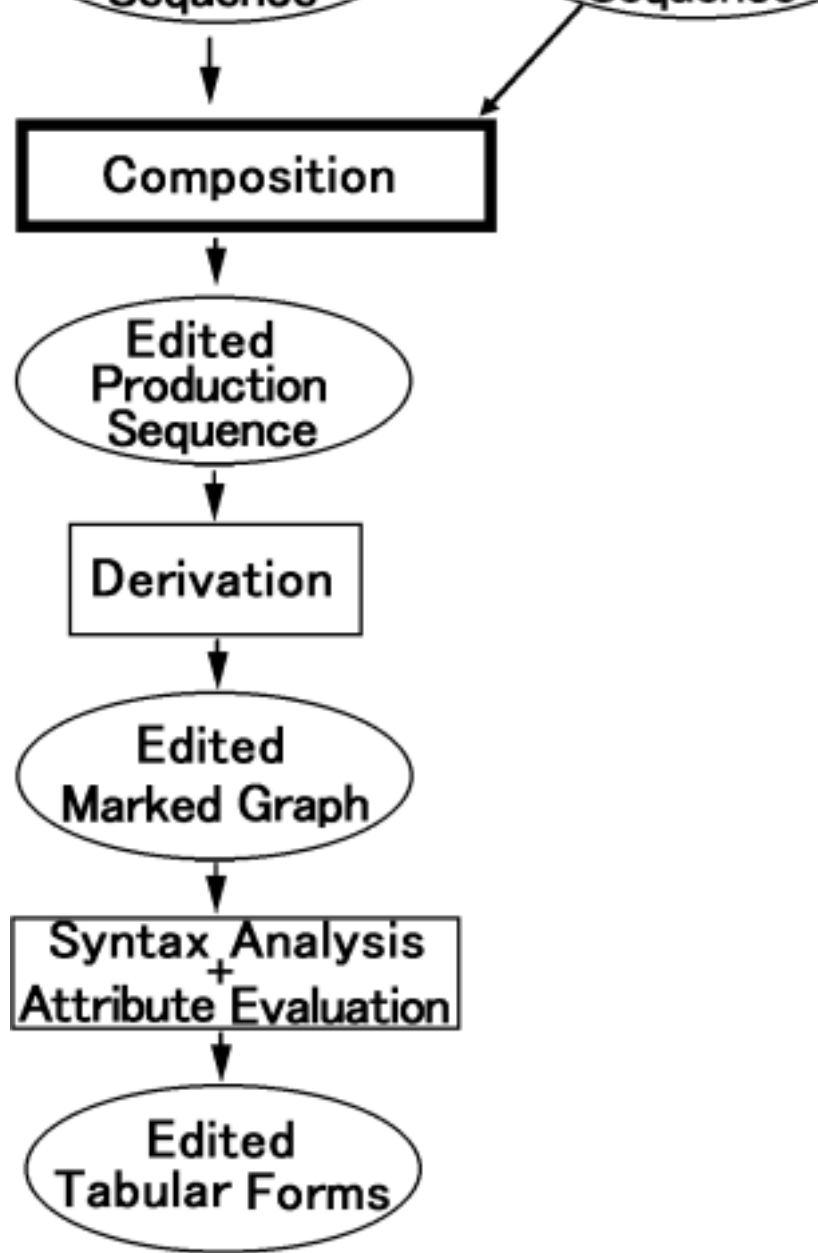
Insertion in HNGG is executed in linear time.





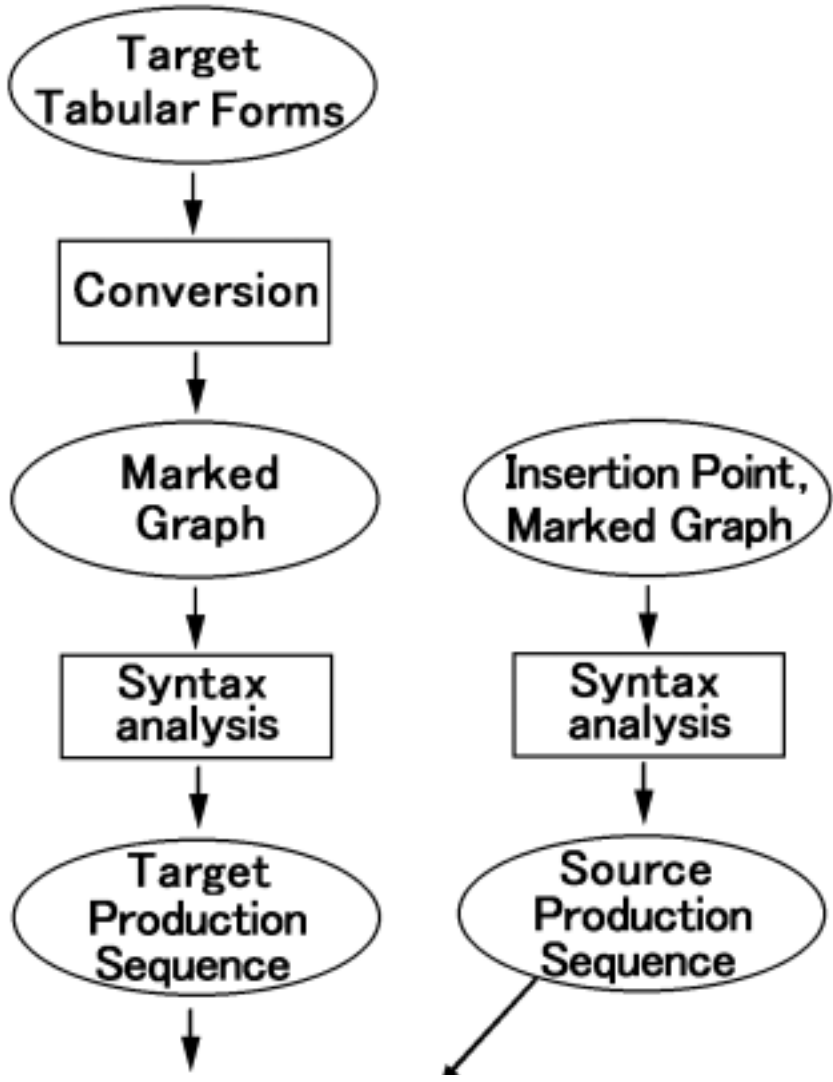
# Derivation Tree of HNGG



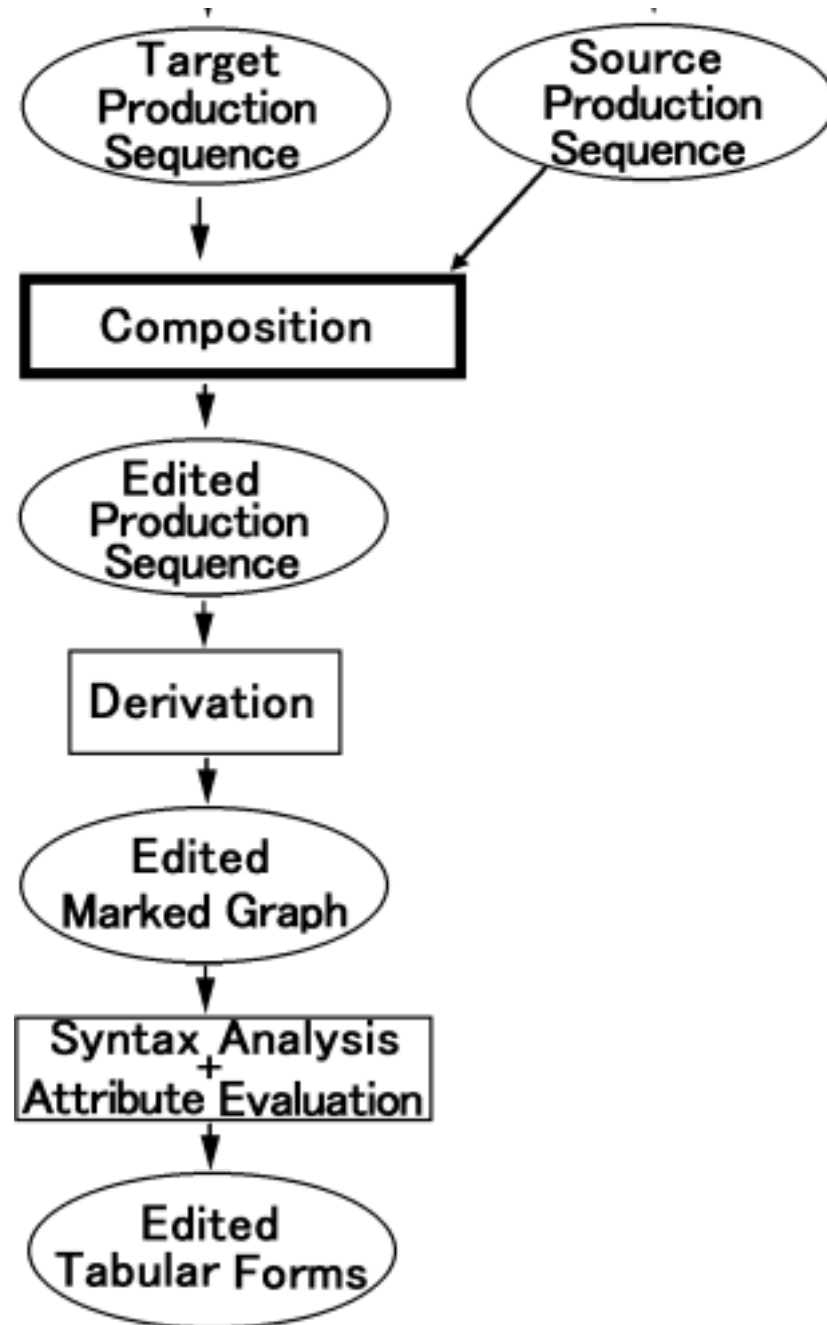


A process flow for an insertion of Hiform editing system

■ Insertion process of editor



■ Insertion process  
of editor (continued)



# 3.3 Syntactic Deletion of Item

## 3.3 Syntactic Deletion of Item

### 3.3.1 Definition (deletable)

For the derivation sequence  $D_0 \xRightarrow[p_1]{H^1p_1} \dots \xRightarrow[p_k]{H^k} F \xRightarrow[p]{H^p} D_p \xRightarrow[p_l]{H^l} \dots \xRightarrow[p_n]{H^{pn}} D_n$ ,

The graph that  $D_p$  has node  $u \in V_D$  for the first time  
Node  $u$  is not applied to any production after that.

Production  $p = X_p (D_p, C_p) \in P_N$  is deletable if one of the following Assumptions 1-3 is met

# Assumption 1

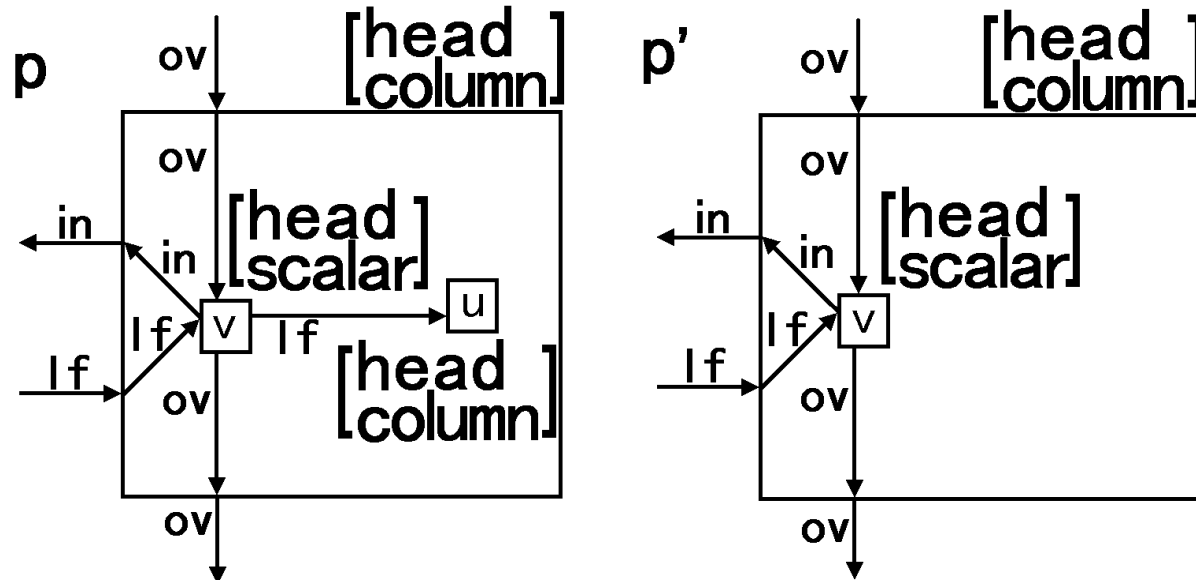
For  $p \in P_N$ ,  $p': X_p \in (D_p, C_p) \in P_N$  s.t.

1 .  $X_{p'} = X_p$

2 .  $H_{p'} \equiv H_p - \{u\}$

3 .  $f, g$  : isomorphic mappings,  $f : V_{H'p} \rightarrow V_{Hp}$ ,  $g : V_{Hp} \setminus \{f(u)\} \rightarrow V_{Hp'}$   
 then  $(\dots, /, y, d) = (\dots, /, g(y), d)$

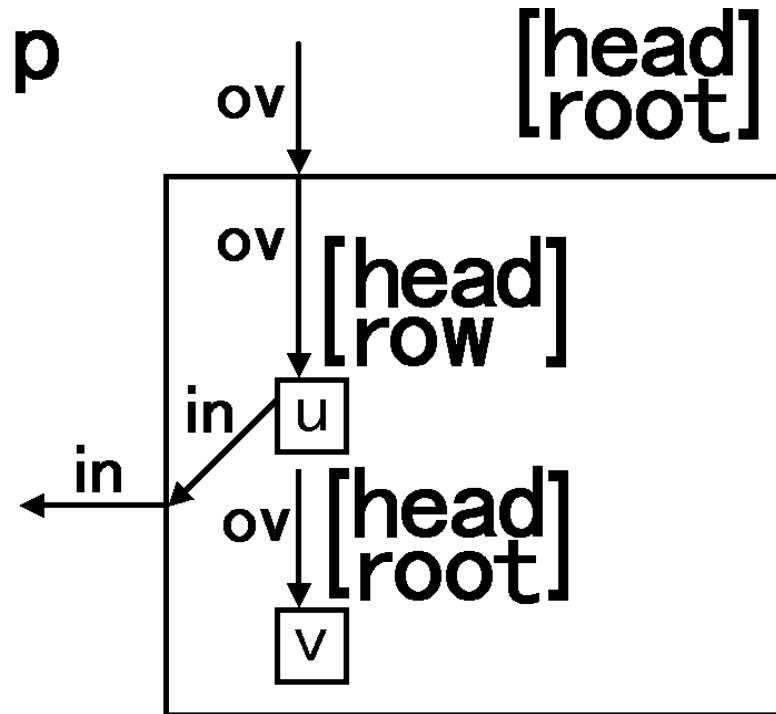
For example:



# Assumption 2

$$V_{H'p} = \{u, v\}, \quad X_{H'p} = H'p(v)$$

For example:

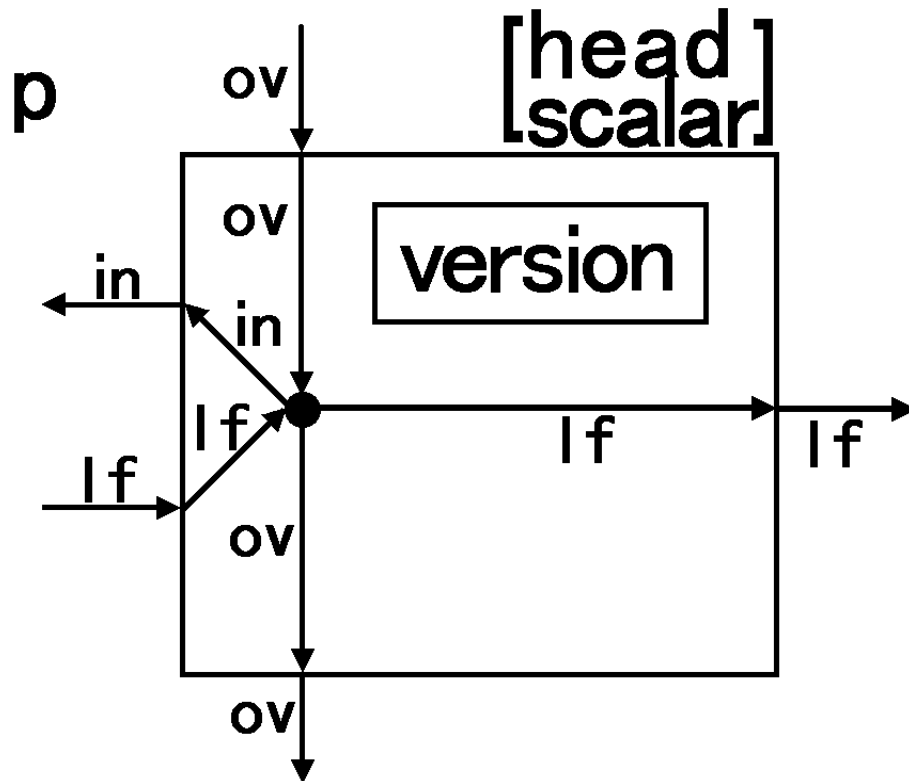




# Assumption 3

$$j \notin H'_p, \quad 1 \leq j \leq n$$

For example:



### Definition 3.3.2

A graph  $H'$  is obtained by syntactic deletion of a node  $A$  from a graph  $H$

*def*

$\Leftrightarrow$

A production  $q$  having a node  $A$  on the right hand side exists.

The production  $q$  is deletable in the instance sequence for graph  $H$ .

$H \cdots H'$ :

$H'$  is the deleted graph which deletes the node  $A$  in the graph  $H$ .

### 3.2.4 Proposition

Let  $H$  be the graph obtained from  $G$  by the deletion of nodes  $a$  and  $b$  in this order, in HNGG.

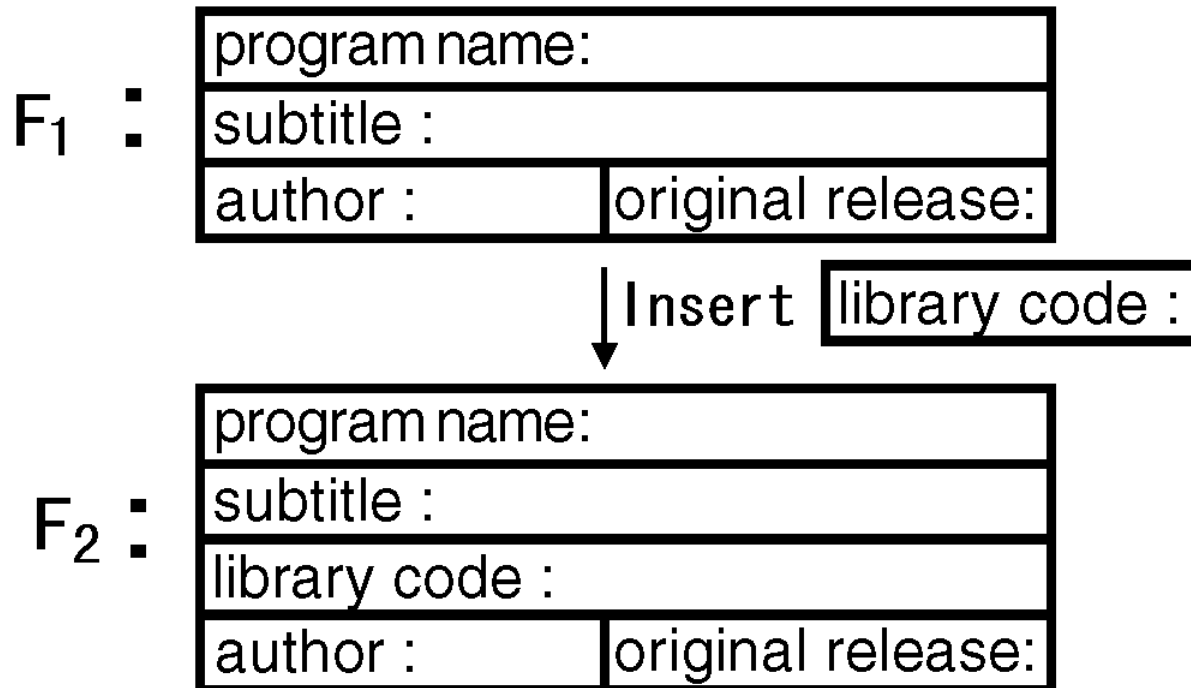
$H'$  be the graph obtained from  $G$  by the deletion of nodes  $b$  and  $a$  in this order, in HNGG.

$H=H'$ .

**Proof.** HNGG has confluence property. Thus, the theorem is verified. □

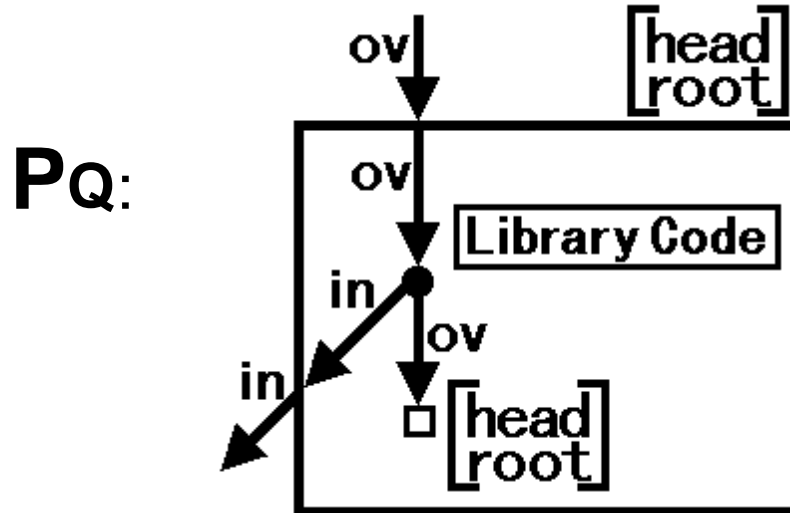
# 4 Example : Insertion Process

Insertion of **library code** between the 2nd and the 3rd branches of F 1



Step1. It makes the composite production copy for the use of the insertion.

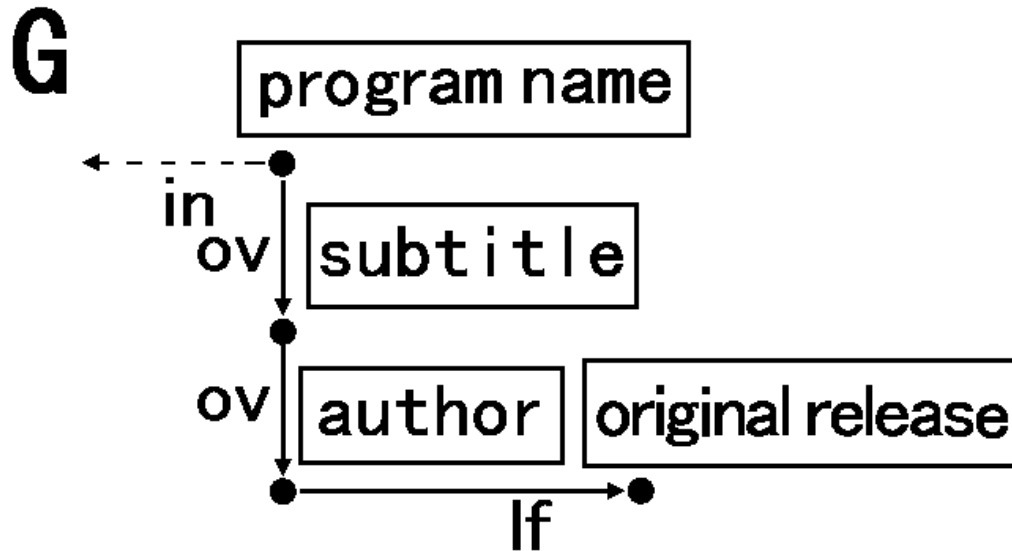
$$PQ = (((P_{H2} P_{H4}) P_{H5}) P_{H6}) P_{H9}) P_{H10}$$



## Step2 Construction of the Derivation D1 of graph G for form F1.

$$\begin{array}{cccccccccccc}
 D_1 : G_0 & \xRightarrow[\rho_1]{H_1 \rho_1} & G_1 & \xRightarrow[\rho_2]{H_2 \rho_2} & G_2 & \xRightarrow[\rho_{H1}]{H_1 H_1 \rho_{H1}} & G_3 & \xRightarrow[\rho_{H2}]{H_2 H_2 \rho_{H2}} & G_4 & \xRightarrow[\rho_{H4}]{H_4 H_4 \rho_{H4}} & G_5 & \xRightarrow[\rho_{H6}]{H_6 H_6 \rho_{H6}} & G_6 & \xRightarrow[\rho_{H7}]{H_7 H_7 \rho_{H7}} & G_7 & \xRightarrow[\rho_{H2}]{H_2 H_2 \rho_{H2}} & G_8 & \xRightarrow[\rho_{H4}]{H_4 H_4 \rho_{H4}} \\
 G_9 & \xRightarrow[\rho_{H6}]{H_6 H_6 \rho_{H6}} & G_{10} & \xRightarrow[\rho_{H8}]{H_8 H_8 \rho_{H8}} & G_{11} & \xRightarrow[\rho_{H3}]{H_3 H_3 \rho_{H3}} & G_{12} & \xRightarrow[\rho_{H4}]{H_4 H_4 \rho_{H4}} & G_{13} & \xRightarrow[\rho_{H5}]{H_5 H_5 \rho_{H5}} & G_{14} & \xRightarrow[\rho_{H11}]{H_1 H_1 \rho_{H11}} & G_{15} & \xRightarrow[\rho_{H6}]{H_6 H_6 \rho_{H6}} & G_{16} & \xRightarrow[\rho_{H13}]{H_1 H_3 \rho_{H13}} & & & 
 \end{array}$$

G

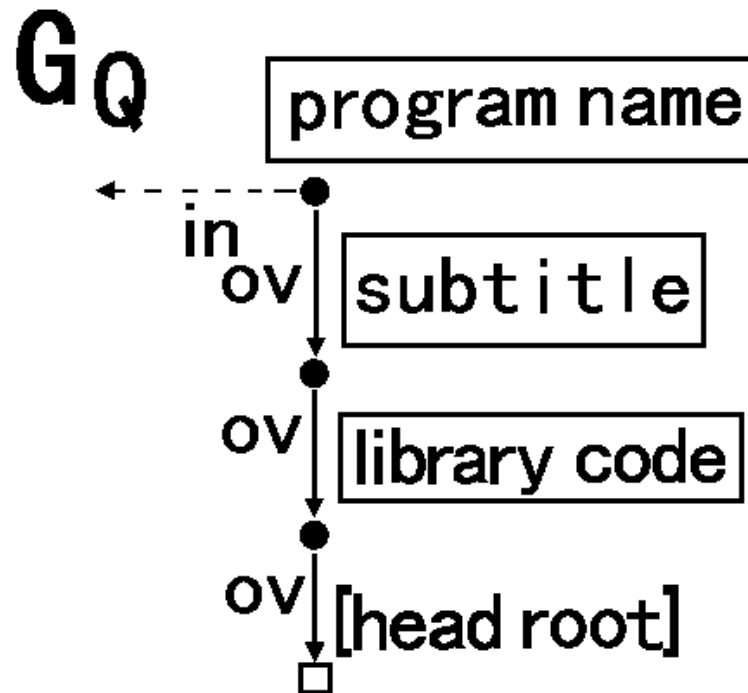




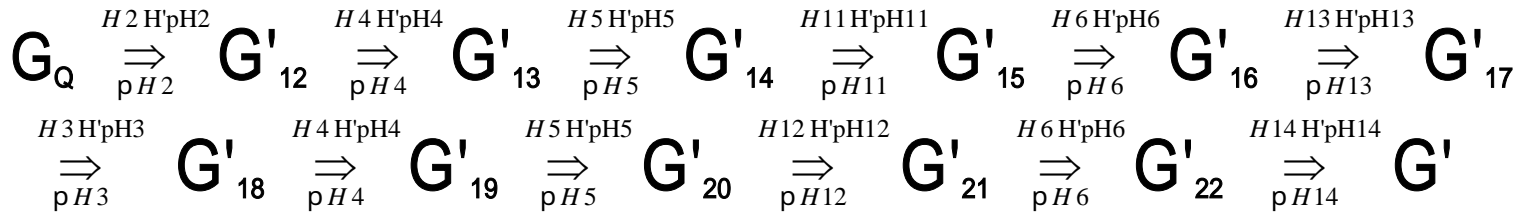


Step4. Apply PQ to G11 and obtain GQ.

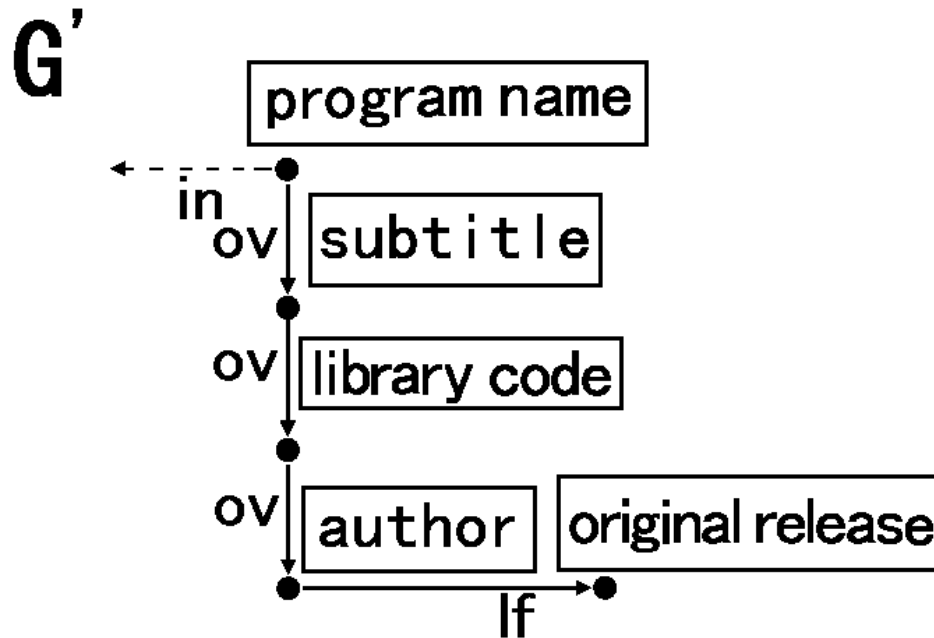
$G_{11} \xrightarrow[\text{pQ}]{\text{QH'pQ}} G_Q$

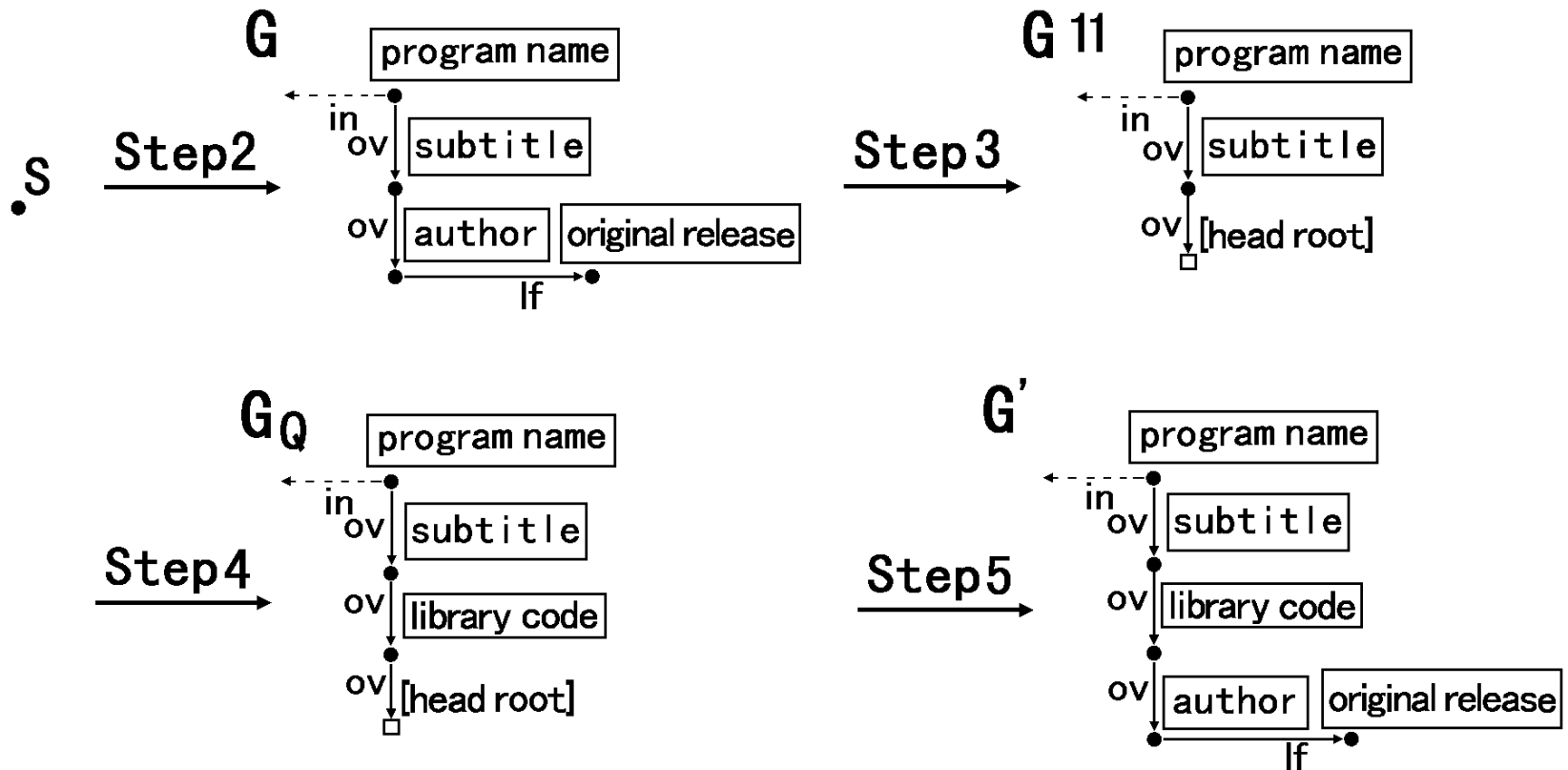


Step5. Apply the latter part of G23 to GQ.

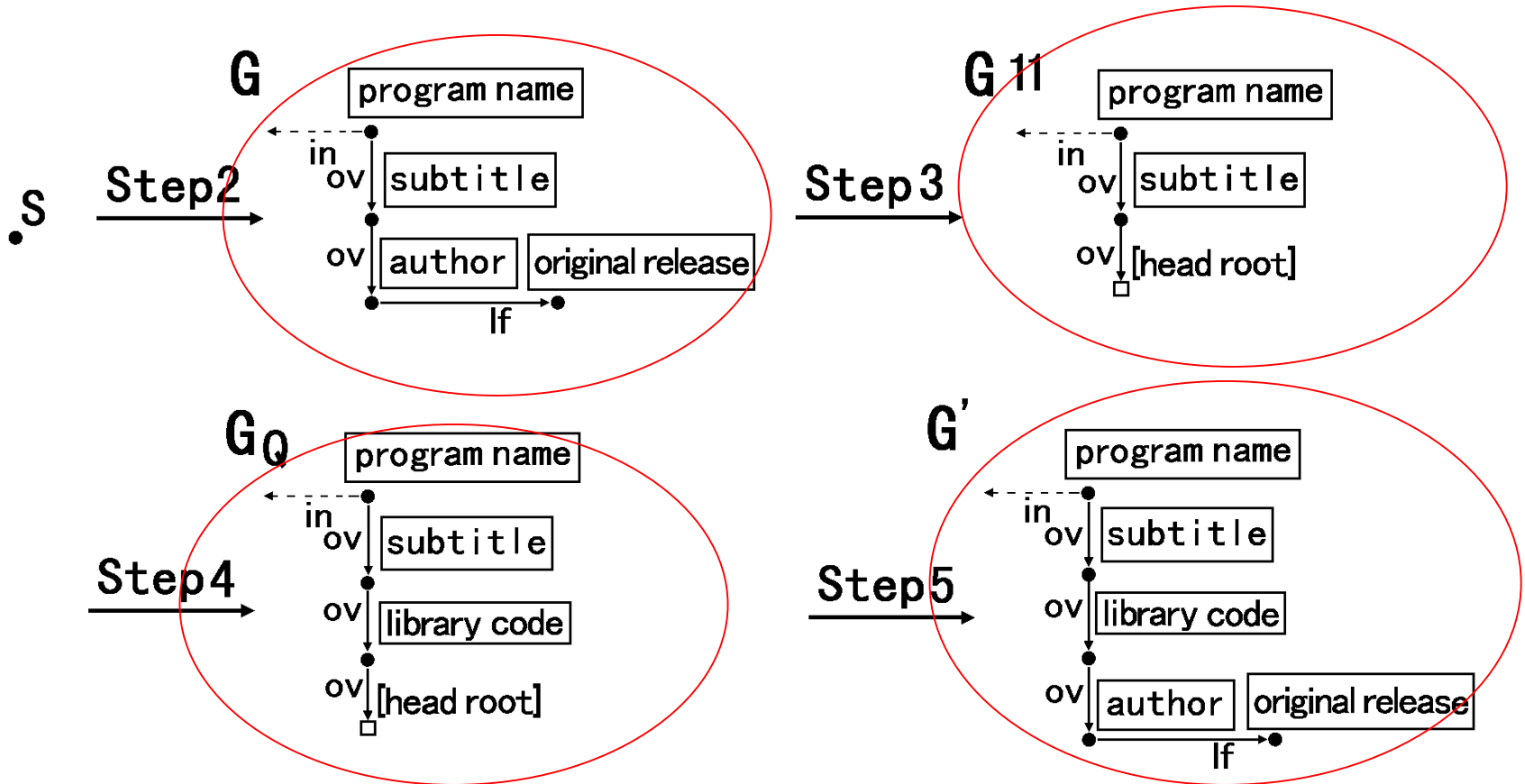
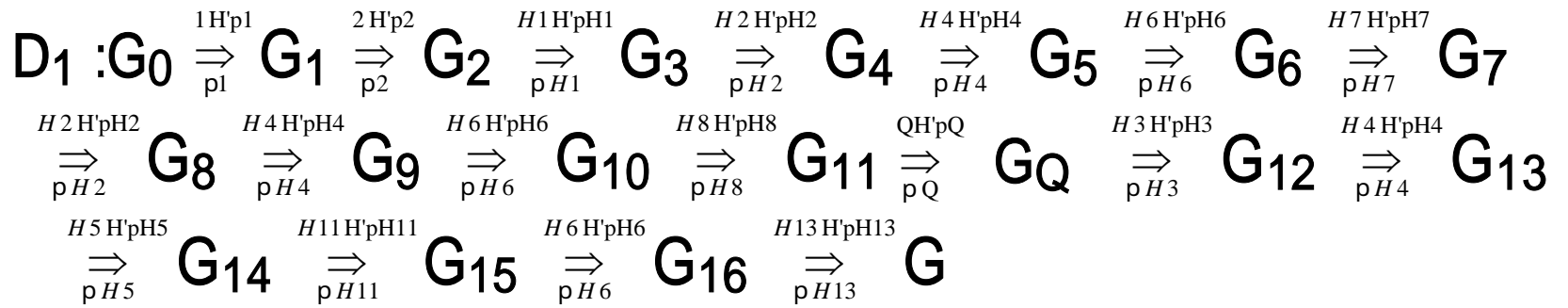


$G'$  is a graph for form  $F_2$ .





Insertion process



Insertion process



# 5. Conclusion

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- We proposed syntactic editing methods for tabular forms, based on the attribute edNCE graph grammar.
  - Insert manipulation (Section 3.2)
  - Delete manipulation (Section 3.3)
- Linear time editing algorithm with attribute rules for primitive drawing

## **Future Works**

- Incremental Algorithm
- Attribute Rules for more sophisticated drawing
- Other edit manipulations representing a division manipulation, a combination manipulation and so on.
- We are now developing a tabular form editor system utilizing this approach.